

## UNIT 4 EXERCISES 6-10

## TRIANGLES

- 2004B 6. Minneapolis-St. Paul International Airport is 8 miles southwest of downtown St. Paul and 10 miles southeast of downtown Minneapolis. Which of the following is closest to the number of miles between downtown St. Paul and downtown Minneapolis?
- (A) 13                      (B) 14                      (C) 15                      (D) 16                      (E) 17
- 2005B 6. In  $\triangle ABC$ , we have  $AC = BC = 7$  and  $AB = 2$ . Suppose that  $D$  is a point on line  $AB$  such that  $B$  lies between  $A$  and  $D$  and  $CD = 8$ . What is  $BD$ ?
- (A) 3                      (B)  $2\sqrt{3}$                       (C) 4                      (D) 5                      (E)  $4\sqrt{2}$
- 2007A 6. Triangles  $ABC$  and  $ADC$  are isosceles with  $AB = BC$  and  $AD = DC$ . Point  $D$  is inside  $\triangle ABC$ ,  $\angle ABC = 40^\circ$ , and  $\angle ADC = 140^\circ$ . What is the degree measure of  $\angle BAD$ ?
- (A) 20                      (B) 30                      (C) 40                      (D) 50                      (E) 60

- 2007B 6. Triangle  $ABC$  has side lengths  $AB = 5$ ,  $BC = 6$ , and  $AC = 7$ . Two bugs start simultaneously from  $A$  and crawl along the sides of the triangle in opposite directions at the same speed. They meet at point  $D$ . What is  $BD$ ?
- (A) 1      (B) 2      (C) 3      (D) 4      (E) 5
- 2016B 6. All three vertices of  $\triangle ABC$  lie on the parabola defined by  $y = x^2$ , with  $A$  at the origin and  $\overline{BC}$  parallel to the  $x$ -axis. The area of the triangle is 64. What is the length  $BC$ ?
- (A) 4      (B) 6      (C) 8      (D) 10      (E) 16
- 2003A 7. How many non-congruent triangles with perimeter 7 have integer side lengths?
- (A) 1      (B) 2      (C) 3      (D) 4      (E) 5
- 2010A 8. Triangle  $ABC$  has  $AB = 2 \cdot AC$ . Let  $D$  and  $E$  be on  $\overline{AB}$  and  $\overline{BC}$ , respectively, such that  $\angle BAE = \angle ACD$ . Let  $F$  be the intersection of segments  $AE$  and  $CD$ , and suppose that  $\triangle CFE$  is equilateral. What is  $\angle ACB$ ?
- (A)  $60^\circ$       (B)  $75^\circ$       (C)  $90^\circ$       (D)  $105^\circ$       (E)  $120^\circ$
- 2009B 9. Triangle  $ABC$  has vertices  $A = (3, 0)$ ,  $B = (0, 3)$ , and  $C$ , where  $C$  is on the line  $x + y = 7$ . What is the area of  $\triangle ABC$ ?
- (A) 6      (B) 8      (C) 10      (D) 12      (E) 14

- 2006B 10. In a triangle with integer side lengths, one side is three times as long as a second side, and the length of the third side is 15. What is the greatest possible perimeter of the triangle?
- (A) 43      (B) 44      (C) 45      (D) 46      (E) 47
- 2007A 10. A triangle with side lengths in the ratio 3:4:5 is inscribed in a circle of radius 3. What is the area of the triangle?
- (A) 8.64      (B) 12      (C)  $5\pi$       (D) 17.28      (E) 18
- 2015B 10. How many noncongruent integer-sided triangles with positive area and perimeter less than 15 are neither equilateral, isosceles, nor right triangles?
- (A) 3      (B) 4      (C) 5      (D) 6      (E) 7